

PHYS 321 TEST1

<1.1>

- 1900, Plank suggest that “energy is radiated and absorbed in quantities divisible by discrete energy element” when he tried to solve “black body radiation” problem introduced by Kirchhoff 1859
- 1905, Einstein postulated that light itself consist of individual quanta and explained photoelectric effect (1839)
- Compton effect

<1.2>

$$a. t = \frac{26.4 \text{ year} \cdot c}{0.99c} = 26.67 \text{ year}$$

$$b. \gamma = \frac{1}{\sqrt{1 - (0.99)^2}} = 7.09$$

$$t' = \frac{t}{\gamma} = 3.76 \text{ year}$$

<1.3>

No.

$$E = \gamma mc^2, \quad p = \gamma mv, \quad \text{where } \gamma \rightarrow \infty \text{ as } v \rightarrow c.$$

<1.4>

$$a. E_m = E_1 + E_2, \quad \vec{p}_m = \vec{p}_1 + \vec{p}_2$$

$$\Rightarrow E_m = (m_1^2 c^4 + p_1^2 c^2)^{\frac{1}{2}} + (m_2^2 c^4 + p_2^2 c^2)^{\frac{1}{2}},$$

$$\vec{p}_m = p_1 \hat{j} + p_2 \hat{i}$$

$$\text{Then } E_m^2 = m^2 c^4 + |\vec{p}_m|^2 c^2$$

$$[(0.25 + 4)^{\frac{1}{2}} + (1 + 2.25)^{\frac{1}{2}}]^2 = 3.86^2 = m^2 c^4 + 6.25$$

$$M = 2.94 \text{ GeV} / c^2$$

$$b. v = \frac{pc^2}{E} = \frac{2.5}{3.86} = 0.65 c$$

<2>

$$a. W = \hbar \omega = \frac{\hbar 2\pi c}{\lambda}$$

$$\lambda = \frac{\hbar 2\pi c}{W} = 652 \text{ nm}$$

$$b. K = \hbar \omega - W = \frac{\hbar 2\pi c}{\lambda} - W = 2.48 - 1.9 = 0.58 \text{ eV}$$

<3>

$$\Delta p = m\Delta v = m \times 43 \times 5\%$$

$$\text{also, } \Delta p \Delta x \geq \frac{\hbar}{2}$$

$$\text{so, } \Delta x \geq \frac{\hbar}{2 \times 43 \times 5\% \times m}$$

$$\Delta x_{\text{baseball}} \geq \frac{\hbar}{2 \times 43 \times 5\% \times 0.15} = 1.64 \times 10^{-34} \text{ m}$$

$$\Delta x_{\text{electron}} \geq \frac{\hbar}{2 \times 43 \times 5\% \times 9.1 \times 10^{-31}} = 2.6 \times 10^{-5} \text{ m}$$

<4>

$$\text{a. } \hbar\omega = \hbar 2\pi f = \Delta E = E_3 - E_1 = hcR\left(\frac{1}{1} - \frac{1}{9}\right) = 13.6\text{eV} \times \frac{8}{9} = 12.09\text{eV}$$

$$f = \frac{12.09\text{eV}}{2\pi\hbar} = 3.1 \times 10^{15} \text{ Hz}$$

$$\text{b. upper limit} = hcR\left(\frac{1}{1} - \frac{1}{\infty}\right) = 13.6\text{eV}$$

$$\text{lower limit} = hcR\left(\frac{1}{\infty} - \frac{1}{\infty}\right) = 0$$